Ultrafast generation and control of an electron vortex beam via chiral plasmonic near fields

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Vortex-carrying matter waves, such as chiral electron beams, are of significant interest in both applied and fundamental science. Continuous-wave electron vortex beams are commonly prepared via passive phase masks imprinting a transverse phase modulation on the electron's wavefunction. Here, we show that femtosecond chiral plasmonic near fields enable the generation and dynamic control on the ultrafast timescale of an electron vortex beam. The vortex structure of the resulting electron wavepacket is probed in both real and reciprocal space using ultrafast transmission electron microscopy. This method offers a high degree of scalability to small length scales and a highly efficient manipulation of the electron vorticity with attosecond precision. Besides the direct implications in the investigation of nanoscale ultrafast processes in which chirality plays a major role, we further discuss the perspectives of using this technique to shape the wavefunction of charged composite particles, such as protons, and how it can be used to probe their internal structure.

he quantum wave nature of both light and matter has enabled several tools to shape them into new wave structures defined by exotic non-trivial spatiotemporal properties¹. Among these techniques, the impartment of a vortex onto their transverse phase profile is having a significant impact in both applied and fundamental science. Vortices are stagnant points at which the phase is undefined, while along a contour around them it varies by an integer multiple m of 2π . The magnitude and sign of the quantization number m, also known as the topological charge, indicate the amount and the handedness, respectively, of the phase cycles surrounding the vortex2. If the singularity is located along the wave's central axis z, it is simply accounted for by a phase factor $\exp(im\phi)$ in the wavefunction, where ϕ is the azimuthal angle. Provided that the modulus of the wave is circularly symmetric, then the presence of this term causes the wave to carry orbital angular momentum (OAM), as it effectively becomes an eigenstate of the z component of the OAM operator with eigenvalue mħ, where ħ is the reduced Planck constant. Vortices have been extensively studied in optical waves within the context of classical and quantum communications³⁻⁵, optical trapping^{6,7}, quantum entanglement^{8,9} and nanostructured plasmonic devices¹⁰. Vortices in electron waves have also become increasingly relevant in modern science, especially in electron microscopy 11-14. Combining the OAM of the vortex beam with the charge of the electrons results in an increased sensitivity to local magnetic properties 15,16. Both optical and electron beams that carry OAM can be produced by means of passive devices that directly modify their wave structure, such as spiral phase plates¹⁷, amplitude holograms¹⁸ and phase holograms^{19,20}. The electron's charge also allows a vortex to be obtained by other methods, such as magnetic needles21, programmable

electrostatic displays²² and tunable electrostatic phase devices²³. Alternative approaches relying on the discrete exchange of OAM between interacting relativistic electrons and optical electromagnetic waves have also been theoretically proposed^{24,25}. However, all experimental implementations so far have been limited to continuous-wave vortex electron beams, restricting the range of possible applications mainly to the investigation of ground-state processes, whereas a huge amount of information resides in the exploration of the non-equilibrium dynamics.

In this Article we show experimentally that ultrafast vorticity can be imparted to charged particles by interaction with strong local electromagnetic fields sustained by collective electronic modes. This is achieved by having ultrashort single-electron wavepackets interacting with an optically excited femtosecond chiral plasmonic near field. This interaction induces an azimuthally varying phase shift on the electron's wavefunction, as mapped via ultrafast transmission electron microscopy^{26,27}. Compared with static approaches using passive phase masks, this method offers a higher degree of scalability to small length scales and a highly efficient dynamic phase control, derived from the ability to manipulate the ultrafast plasmonic field. We demonstrate this level of phase manipulation using a sequence of two phase-locked light pulses to coherently control the properties of the vortex beam with attosecond precision. Our experimental results are described by means of a general theoretical framework that can also be applied to other charged particles and thus potentially to other matter waves such as proton beams. The ability to add OAM onto the latter could have fundamental implications for open questions in hadronic physics, where OAMcarrying protons could be used to address the origin of their spin (the proton spin puzzle)²⁸.

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Several recent studies have shown that a strong longitudinal phase modulation of the electron wavefunction can be achieved by interaction with intense optical fields²⁹⁻³¹. Given that imparting OAM relies on modulation of an electron's transverse phase profile, a crucial aspect for experimental realization is the ability to synthesize an optical field with a well-defined chirality that would extend over the transverse plane and be efficiently confined on the length scale defined by the electron transverse coherence (on the order of ~1 µm for femtosecond electron pulses). The usually adopted configurations are, however, not suitable for this task because the spin of the photon, as defined by its circular polarization, cannot be directly mapped into the OAM of the electron in a simple electron-photon interaction process, such as in inverse transition radiation. The interaction thus needs to rely on the interruption of light propagation by a scattering object able to create a spatially confined OAM-carrying optical field. This condition can be generated by the excitation of chiral surfaceplasmon polaritons (SPPs)32-34, which relies on the spin-to-OAM conversion from circularly polarized light in non-paraxial scattering and is a clear manifestation of the strong spin-orbit coupling of light when confined to subwavelength scales^{33,34}. When a circularly polarized light beam encounters a properly designed nanoscale cavity, it is able to scatter into in-plane SPPs with a non-zero topological charge and helical phase distribution³³. For a cylindrically symmetric structure, conservation of the total angular momentum quantum number restricts the plasmon OAM to be only $+\hbar$ or $-\hbar$ according to the helicity of the incident light plane wave. Arbitrarily large values of plasmon OAM are instead possible by using incident light with high vorticity (for example, Bessel beams).

We generated a chiral plasmonic field by illuminating a nanofabricated hole in a Ag film deposited on a Si₃N₄ membrane (diameter of ~0.8 μm) with circularly or partially circularly polarized light carrying energy of $\hbar\omega = 1.57 \,\text{eV}$ per photon (Fig. 1a). SPPs are generated at the hole edge and radially propagate away within the Ag/ Si₃N₄ interface with a phase distribution that can be directly mapped by means of a non-local holographic method³⁵. The latter directly draws from a recently developed approach used to homogeneously modulate the phase of the electron wavefunction by means of a semi-infinite light field obtained when a nearly plane-wave light beam is reflected from a continuous Ag layer (opaque to the light but semi-transparent to the electrons)31. In the presence of a nanostructure, this effect would generally coexist with electron scattering from the local field of the photo-excited SPP propagating at the Ag/ Si₃N₄ interface, which is phase-locked with the light field reflected at the Ag surface. The electron wavepacket can thus coherently interact with both fields (light and SPPs) while traversing the structure. The resulting position-dependent interference between the semiinfinite light field and the SPP field gives rise to a spatially oscillating field amplitude that directly translates into a modulation of the electron wavefunction that can be imaged in real space (Fig. 1b). This interference mechanism thus allows us to directly access the phase distribution of the plasmon field itself. This is experimentally obtained by energy-filtered imaging, where we selectively collect only those electrons that have exchanged energy with the optical fields, directly providing the spatial distribution of the inelastically scattered electrons (for further details see Methods).

The inelastically scattered map measured for an elliptically polarized optical illumination when electron and light wavepackets are in temporal coincidence is shown in Fig. 1c and displays the characteristic spiral phase pattern of a chiral SPP. This pattern is in agreement with the finite-difference time-domain (FDTD) simulations shown in Fig. 1e (for further details see Supplementary Section 3). The simulated phase profile of the electric field along the z axis (Fig. 1e) exhibits a clear spiral distribution that resembles the experimental image. Moreover, the simulations clearly show that the SPP field displays, in the centre of the hole, a phase singularity of topological charge m=1. This suggests that a 2π phase shift

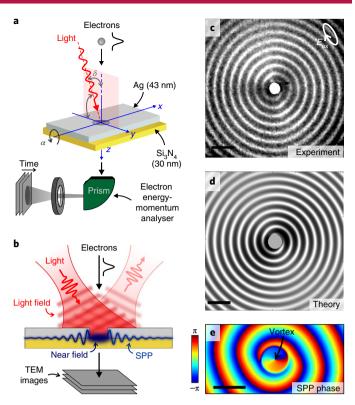


Fig. 1 | Generation and detection of chiral SPPs. a, Schematic representation of the experimental geometry. Ultrashort 200 keV electron pulses (propagating along the z axis) impinge on a Ag/Si₃N₄ thin film perforated by a nanofabricated hole in the Ag layer (diameter ~0.8 μm). Light pulses propagate with their wavevector in the y-z plane forming an angle $\delta = 4.5^{\circ}$ with the electron beam direction. The sample can rotate around the x axis by an angle α . An electron energy-momentum analyser allows us to measure the transverse profile of the electron wavefunction in both real and reciprocal space. **b**, Schematic representation of the non-local holographic method used to image SPPs radially propagating at the Ag/Si₃N₄ interface away from the hole. **c**, Experimentally measured spatial distribution of the inelastically scattered electrons following the electron-plasmon interaction. The image is acquired with electrons and light wavepackets in temporal coincidence. The sample is tilted by an angle $\alpha = \delta$ to achieve normal light incidence. The image reveals the spiral phase pattern typical of a chiral plasmon generated by illumination with an elliptically polarized light field (scale bar, 2 μm). d, Calculated real-space electron intensity distribution using the semi-analytical theory detailed in the text and the Supplementary Information (scale bar, 2 µm). e, Simulated phase map of the z component of the total electric field at the Ag/Si₂N₄ interface obtained from FDTD simulations (scale bar, 1µm).

can be imprinted onto the electron's wavefunction, provided that it coherently encloses the hole upon propagating through the device.

Further insights can be obtained with a semi-analytical theory. Upon propagation through the plasmon-supporting structure, the incident electron wavefunction $\psi_{\rm inc}(R,\phi,z,t)$ gains inelastically scattered components:

$$\psi_{\ell}(R, \phi, z, t) = \psi_{\text{inc}}(R, \phi, z, t)J_{\ell}(2 |\beta|)$$

$$\times \exp(i\ell \arg\{-\beta\} + i\ell\omega(z/v - t))$$
(1)

labelled by the integer ℓ , which corresponds to the number of plasmons absorbed/emitted by a single electron. A detailed,

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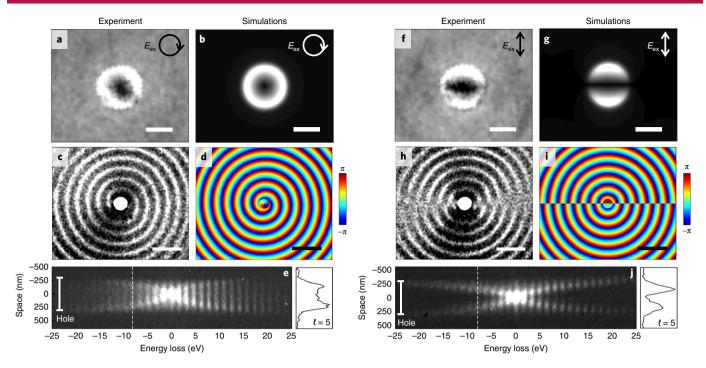


Fig. 2 | One-to-one correspondence between the complex SPP optical field and the transverse distribution of the electron wavefunction. **a,f**, Experimentally measured spatial distribution of the inelastically scattered electrons inside the hole after subtraction of the corresponding energy-filtered map without laser excitation (see also Supplementary Fig. 3) for both circularly polarized (**a**) and linearly polarized (**f**) optical illumination (scale bar, 0.5 μm). **b,g**, Simulated spatial distributions of the interaction strength | β | for the two polarization states. A zero-field region with cylindrical or mirror symmetry is visible inside the hole when circularly (**b**) or linearly (**g**) polarized light is used (scale bar, 0.5 μm). **c,h**, Spatially oscillating pattern measured outside the hole for the two polarizations (scale bar, 2 μm). **d,i**, Simulated spatial distribution of the phase of β within the x-y plane (scale bar, 2 μm). **e,j**, Space-energy maps measured for the two polarization states (circular (**e**) and linear (**j**)) showing the modulation of the spatial distribution of the scattered electrons inside the hole as a function of the order ℓ of absorbed/emitted SPPs.

self-contained derivation of this expression is given in ref. 31. Here, R and ϕ are the transverse cylindrical coordinates centred at the hole, ν is the electron velocity, and I_{ℓ} is the ℓ th-order Bessel function of the first kind. All of these scattered components are fully described in terms of a single complex function $\beta(R,\phi)$, which captures the interaction of the electron with the light and SPP fields. As detailed in Supplementary Section 2, the interaction strength is determined by the electric field component along the z axis³¹, which in our case can be written as $\beta \sim A + B\exp(ik_{SPP}R)$, where the first term represents the interaction of the electrons with the semi-infinite light field (reference) and the second term defines the interaction with the SPP field propagating with a wavevector k_{SPP} (signal). A direct comparison between theory and experiment can be obtained for the real-space electron intensity distribution shown in Fig. 1d (see Supplementary Section 2 for details), which nicely reproduces the experimental data.

This one-to-one correspondence between the complex optical field of the SPP and the transverse distribution of the electron wavefunction is further evidenced in Fig. 2 by comparing experiments and FDTD simulations for both circularly polarized and linearly polarized light illumination. In Fig. 2a,f we show the experimentally measured spatial distribution of the inelastically scattered electrons inside the hole after subtraction of the corresponding energy-filtered map obtained without laser excitation (Supplementary Fig. 3). The resulting images, obtained for both polarization states, directly correlate with the simulated spatial distribution of the modulus of β reported in Fig. 2b,g. A zero-field region with cylindrical or mirror symmetry is visible inside the hole when circularly or linearly polarized light is used, respectively. The spatially oscillating pattern measured outside the hole for the two polarizations (Fig. 2c,h) is instead a direct representation of the spatial distribution of the phase of β

within the x-y plane (see simulations in Fig. 2d,i). Because the plasmon order ℓ also strongly defines the degree of interaction with the SPP field, the spatial distribution of the scattered electrons can be significantly modulated by ℓ . This can be clearly seen in the space-energy maps shown in Fig. 2e,j for circular and linear polarizations, respectively, where the zero-field region spreads in size with an increasing number of absorbed/emitted SPPs.

We note that, for incident light with circular or partially circular polarization, the phase of the interaction strength β evolves nearly linearly with ϕ (that is, $\arg\{\beta\} \propto \phi$; Supplementary Fig. 4). This linear dependence translates into an overall phase factor $\exp(\pm i\ell\phi)$ in the wavefunction ψ_{ε} , which therefore carries an OAM of $\pm \ell \hbar$ (see also schematics in Fig. 3a). On a fundamental level, the transfer of such phase profile relies on the incident light field creating plasmons with OAM of $\pm m\hbar$. In our case m is equal to 1 due to the axial symmetry of the circular hole and to the $\pm \hbar$ units of the spin angular momentum carried by the circularly polarized Gaussian beam illuminating it. In a general case, the exchange of ℓ plasmons with the electron would thereafter result in a net transfer of $\pm \ell m\hbar$ units of OAM. The use of non-axially symmetric structures sustaining chiral SPPs with arbitrarily large values of m, such as spiral plasmonic lenses^{33,36,37}, is therefore a promising route to create high-OAM vortex electron beams. Because of the linearity of the interaction, our approach works at any value of the incident light intensity and it is thus intrinsically robust with respect to the external parameters. Naturally, the efficiency of the process (that is, the maximum ℓ that can be efficiently reached) might be different according to the extent of the photoexcitation.

To further verify the OAM transfer, we also monitored the farfield images of the electron beam in the transverse-momentum space (k_x,k_y) , and determined the changes produced by the presence

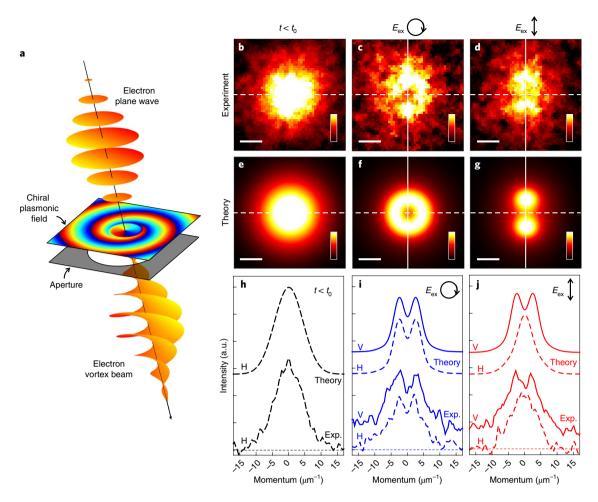


Fig. 3 | Generation and detection of an ultrafast electron vortex beam via interaction with a chiral plasmonic near field. **a**, Schematic representation of OAM transfer to electrons. The interaction between a pulsed electron plane wave synchronized with a chiral plasmonic field creates an OAM-carrying electron wavepacket. **b-d**, Experimentally measured far-field images of the electron beam in the transverse-momentum space before laser illumination (**b**) or in the presence of circularly polarized light (**c**) and linearly polarized light (**d**) (scale bars, $4 \mu m^{-1}$). The images are acquired with electron and light wavepackets in temporal coincidence. The experimental geometry (and in particular the angle α) is chosen such that the interaction of the electrons with the incident and reflected light beams vanishes while maintaining a significant coupling with the plasmonic near field. **e-g**, Calculated reciprocal-space intensity distribution of the electron beam using the analytical theory and the FDTD simulations described in the text for both circular (**f**) and linear (**g**) light polarization states. The momentum-resolved electron wavefunction $\Psi_{\ell}(k_x, k_y)$ is obtained as the Fourier transform of the real-space wavefunction $\psi_{\ell}(k, \phi)$ given by equation (1), where the interaction strength β originating at the hole is extracted from the FDTD simulations (scale bars, $4 \mu m^{-1}$). In **e**, β = 0 is considered to mimic the absence of illumination. In **f** and **g**, the total intensity map is shown as obtained by incoherently adding all the contributions with different values of ℓ . A small momentum broadening is also included to take into account the experimental resolution. **h-j**, Vertical and horizontal line profiles across the central part of the far-field images shown in **b-d** (experiment) and **e-g** (theory).

of illumination. This is shown in Fig. 3c,i for a circularly polarized light beam in combination with a sample orientation that vanishes the electron-light interaction while maintaining a significant electron-plasmon coupling (Supplementary Section 2). Comparison between the reciprocal-space map measured under these conditions (Fig. 3c,i) and that acquired before optical illumination (Fig. 3b,h) reveals a characteristic destructive interference region at the electron beam centre, which attests to the presence of a phase singularity in its transverse phase profile. We attribute the origin of this behaviour to the chiral near field created at the hole, which dominates the coupling with the electron wavepacket (Supplementary Fig. 8) and imprints on it a $2\pi\ell$ phase shift as inherited by the circularly polarized optical illumination. To confirm that the reciprocal-space distribution of the electron beam is indeed determined by the phase profile of the optical field at the hole, we performed additional experiments using a linearly polarized light beam. This is

shown in Fig. 3d,j, where a characteristic two-lobed electron beam ³⁸ is formed as a result of the uniform π phase shift generated across the hole (Fig. 2i).

Within this scenario, the momentum-resolved electron wavefunction $\Psi_{\ell}(k_x, k_y)$ can be calculated as the Fourier transform of the real-space wavefunction $\psi_{\ell}(R, \phi)$:

$$\Psi_{\ell}(k_x, k_y) = \int_{-\pi}^{\pi} d\phi \int_{0}^{+\infty} R dR \exp(-i\mathbf{k}_{\perp} \cdot \mathbf{R}) \psi_{\ell}(R, \phi)$$
 (2)

where $\mathbf{k}_{\perp} = (k_x,k_y)$. Here, $\psi_{\ell}(R,\phi)$ is given by equation (1), where the incident wavefunction $\psi_{\text{inc}}(R,\phi)$ has a lateral extension determined by the electron transverse coherence (~0.7–1 µm), and the interaction strength β originated at the hole is extracted from FDTD simulations where the actual spatial distribution of the near field is

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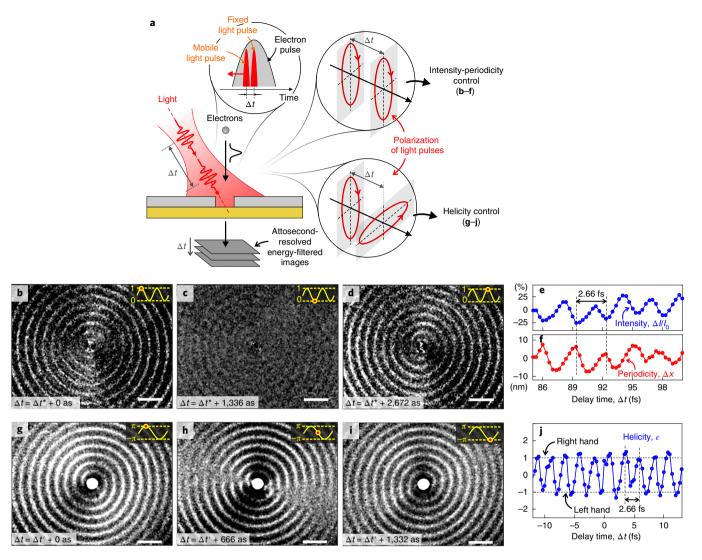


Fig. 4 | Dynamic phase control of the electron/chiral-plasmon interactions. a, Sketch of the two phase-locked light pulses with independent polarization states and variable relative delay time Δt used to coherently launch two interfering chiral SPPs at the edge of the hole. Here, the sample is tilted to have normal light incidence ($\alpha = \delta$). **b-f**, Experimentally measured spatial maps of the inelastically scattered electrons (**b-d**) as a function of Δt (varied in steps of 334 as) when the two light pulses are elliptically polarized with parallel major axes and initially separated by $\Delta t = 85$ fs (scale bars, 2 μm). The plots show the difference between the maps acquired at $\Delta t^* = 94$ fs and at $\Delta t > \Delta t^*$. The result is a coherent modulation of the intensity (**e**) and of the spatial periodicity (**f**) of the plasmonic fringes with a temporal period of ~2.67 fs. **g-i**, Experimentally measured spatial maps of the inelastically scattered electrons (**g-i**) as a function of Δt when using two elliptically polarized light pulses with major axes perpendicular to each other and initially separated by $\Delta t = -12$ fs (scale bars, 2 μm). The plots show the real-space maps acquired at $\Delta t' = -4.35$ fs and at $\Delta t > \Delta t'$. In this configuration, the sign of the topological charge (helicity) of the phase singularity created at the hole is observed to switch from positive to negative within each optical cycle.

considered (Supplementary Fig. 8). The total Fourier-plane intensity is then obtained as

$$I_{\mathrm{F}}(k_{x},k_{y}) = \sum_{\ell=-\infty}^{+\infty} |\Psi_{\ell}(k_{x},k_{y})|^{2}$$

The calculated maps, where a small momentum broadening is also included to take into account the experimental resolution, are shown in Fig. 3e–g and correctly reproduce the doughnut-shaped and two-lobed probability distributions observed in the experiment as induced by the chiral and linear transverse phase modulation, respectively. Our experimental and theoretical results are also in excellent agreement with standard electron vortex beam calculations (for details see Supplementary Section 4). In the latter case,

the effect of the chiral near field on the electron wavefunction is simulated by the interaction of a plane wave with a spatially confined spiral phase plate of order ℓ , whose extension is determined by the hole diameter (Supplementary Fig. 10).

An extremely interesting feature of our approach is the ability to dynamically control the vortex beam properties. This is possible thanks to the high degree of tunability of the optical field, which allows us to coherently modulate the longitudinal and transverse phase profile of the electron wavefunction. This is achieved by manipulating the phase distribution of the plasmonic near field with attosecond precision using a sequence of two phase-locked 55 fs light pulses with a relative delay, Δt , between them varied in steps of 334 as (see also ref. 31). As schematically depicted in Fig. 4a, this three-pulse scheme allows us to finely control the relative phase of the two optically excited plasmons. In the first implemented

configuration we have used two elliptically polarized light pulses with parallel major axes. The initial delay was set to $\Delta t^* = 85$ fs, longer than their cross-correlation, to minimize the optical interference between the two pulses, which remained nevertheless below a 5×10^{-2} level. When varying the delay time between the two optical pulses, the observed time-dependent evolution of the plasmonic pattern is a sequence of constructive and destructive interference between the optically generated plasmons propagating at the Ag/Si₃N₄ interface (Fig. 4b-d). The result is a coherent modulation of the intensity and of the spatial periodicity of the plasmonic fringes with a temporal period given by the optical cycle of ~2.67 fs (Fig. 4e,f, Supplementary Video 1 and calculations in Supplementary Fig. 6). This effect, which cannot be related to a simple optical interference within the incident light field, can be understood as the coherent interaction between two spatially and temporally localized plasmon wavepackets. In a second configuration, the elliptical polarization of the two light pulses is arranged such that their major axes are perpendicular to each other. In this way, we effectively have a dynamic handle on the helicity of the phase singularity created at the centre of the nanofabricated hole. This is shown in Fig. 4g-i and in Supplementary Video 2 (see also calculations in Supplementary Fig. 7), where the handedness of the spiral plasmonic phase distribution is observed to switch from clockwise to anticlockwise within each optical cycle when varying Δt . The observed periodic modulation of the helicity of the plasmonic pattern is shown in Fig. 4j, and shows the ability to control with attosecond precision the sign of the topological charge of the electron vortex beam created by the electron-plasmon interaction.

With respect to commonly adopted methods using passive phase masks to produce electron vortex beams, our approach is intrinsically scalable to smaller length scales in the subwavelength regime (Supplementary Fig. 9). This is extremely interesting in situations where only a partial transverse coherence of the beam can be achieved (such as in the case of ultrashort electron pulses). This is even more crucial when our laser-based method for transferring OAM is extended to pulsed beams of heavier elementary and composite charged particles, where the constraint on the lateral coherence becomes stricter and limited to less than a few tens of nanometres. In particular, imparting OAM in composite particles could be of interest for analysing their internal structure³⁹.

When considering a proton, by shaping its wavefunction in a manner similar to that demonstrated here for electrons, the proton can acquire OAM-dependent density functions that will reflect its internal properties on the transverse spatial distribution. One would expect the OAM-carrying proton to behave differently in experiments whose outcome can conventionally be interpreted based only on its fixed agglomeration of partons (quark and gluons). Recently, increasing efforts have been devoted to gaining an understanding of the proton spin in terms of its constituent particles²⁸. The perspective of adding OAM to the proton partons, in conjunction with relativistic spin-orbit effects in matter waves, could be of potential use to these studies11,40. One such study we can now envisage would involve measurements of the magnetic dipole moment for an OAM-carrying proton. This quantity could be approximated based on a semi-classical current density obtained from the proton internal charge density and from the probability current density of its OAM-carrying wavefunction. As quantitatively described in Supplementary Fig. 11, the more the transverse component of the proton wavefunction approaches its internal charge density, the more the proton internal structure affects its magnetic moment. In the opposite limit, when the transverse extension of the wavefunction significantly exceeds the scale of the internal features of the proton, the influence of the internal charge density quickly averages out, thereby yielding a magnetic moment equal to $\ell \mu_N$ typical of a point-like particle with nuclear magneton $\mu_{\rm N}.$ Several schemes could be used to measure such a quantity, including a Stern-Gerlach-like

approach⁴¹ or devices that couple the OAM of a charged particle with its spin^{42,43}. The latter would be extremely valuable for probing the proton internal spin dynamics by means of OAM impartment, thus potentially unravelling the role played by the OAM of its inner constituents in the determination of its total spin.

Online content

Any methods, additional references, Nature Research reporting summaries, source data, statements of code and data availability and associated accession codes are available at https://doi.org/10.1038/s41563-019-0336-1.

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Author contributions

G.M.V., G.B., I.M., E.C., F.J.G.d.A. and E.K. conceived and designed the research. G.M.V., G.B., I.M. and E.P. conducted the experiments and analysed the data. R.J.L., D.M., I.M. and G.M.V. fabricated the samples. F.J.G.d.A. developed the semi-analytical theory and performed the calculations. P.B. performed the FDTD simulations. V.G. performed the electron vortex beam calculations. H.L. and E.K. performed the proton vortex beam calculations. G.M.V., G.B., I.M., O.R., I.K., B.B., V.G., E.K., F.J.G.d.A. and F.C. interpreted the results. All authors contributed to writing the article, and read and approved the final manuscript.

Competing interests

The authors declare no competing interests.

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Methods

The sample sustaining surface-plasmon polaritons (SPPs) was made of a 43-nm-thick ($\pm 5\,\mathrm{nm}$) Ag thin film sputtered on a 30 nm Si $_3\mathrm{N}_4$ membrane. A nanofabricated hole (diameter of ~0.8 $\mu\mathrm{m}$) was milled in the Ag layer using a raster-scanned focused-ion beam (FEI Nova Nanolab 200 focused ion beam/scanning electron microscope) with typical beam currents of ~10 pA at 30 kV voltage. The bilayer was supported by a Si TEM window with a 80×80 $\mu\mathrm{m}^2$ aperture, which was in turn mounted onto a double-tilt sample holder that ensured rotation around the x-axis by an angle α over a $\pm 35^{\circ}$ range (Fig. 1a).

The experiments were performed using an ultrafast transmission electron microscope as sketched in Supplementary Fig. 1 and also detailed in refs. ²⁶ and ²⁷. Femtosecond electron pulses were generated by photoemission from an ultravioletirradiated LaB₆ cathode, accelerated to an energy E_0 = 200 keV along the z axis and then directed onto the specimen surface with parallel illumination. The sample was simultaneously illuminated with femtosecond laser pulses of $\hbar\omega$ = 1.57 eV central energy and variable duration, intensity and polarization state. For the experiments presented in the main text we used a peak amplitude of light field of ~8× 10⁷ V m⁻¹. The light pulses were focused onto the sample surface in a spot size of ~58 µm (full-width at half-maximum). The direction of light propagation was within the y–z plane and formed an angle δ of ~4.5° with respect to the z axis (Fig. 1a). The delay between electrons and photons was varied via a computer-controlled delay line. For the three-pulse experiment, we implemented a Michelson-like interferometer along the optical path of the near-infrared beam, incorporating a computer-controlled variable delay stage along one arm.

The transmission electron microscope was also equipped with a Gatan imaging filter camera for energy-filtered real-space and reciprocal-space imaging and spectroscopy. Real-space images presented in this work were acquired in energy-filtered mode by selecting a $\sim 4-5\,\mathrm{eV}$ window at the centre of a $\sim 6-8\,\mathrm{eV}$ zeroloss peak (ZLP). This allowed us to monitor the depletion of the ZLP following the plasmonic excitation and directly provided the spatial distribution of the inelastically scattered electrons from the optically excited plasmonic near fields (for further details see ref. $^{4+}$). The data presented in Fig. 2a,f, which shows an

experimental measure of the interaction strength within the hole, were obtained by subtracting two energy-filtered images obtained with and without the pump laser excitation (Supplementary Fig. 3). This was necessary for a proper comparison with the simulated interaction strength maps shown in Fig. 2b,g. The space–energy maps in Fig. 2e,j and the spectrum in Supplementary Fig. 2 were acquired in spectroscopy mode using a ~ 1 eV ZLP.

High-dispersion diffraction (HDD) experiments were performed at a camera length of 80 m on a retractable charge-coupled device camera before the electron energy spectrometer. In the reciprocal-space maps shown in Fig. 3 the transverse momentum was defined as $2\pi/distance$, and the scale bar was calibrated by static electron diffraction through a square silicon grating with lateral period of 463 nm. Both real-space images (Figs. 1, 2 and 4) and far-field images (Fig. 3) presented in the main text were acquired in temporal coincidence between the maxima of electrons and light wavepackets. During the HDD experiments we used a micrometre-sized circular aperture (projected radius of 7.5 µm) placed in close proximity to the image plane and centred around the hole. This procedure, together with the low electron transmissivity (~0.013) through the continuous metal film surrounding the hole, guaranteed that a significant portion (~30%) of the electrons reaching the detector at small diffraction angles did indeed interact with the chiral field in the hole (see Supplementary Section 4 for further details). Those electrons that crossed the thick Ag region instead underwent scattering from the SPPs radiated from the hole and mainly contributed to the diffraction pattern with a wide background at higher angles.

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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